

P.G. Sem. IIIrd

Core course X

Rotational Spectroscopy

Unit I: The rotation of molecules

~~Classification~~

The rotation of a three dimensional body may be quite complex and it is convenient to resolve it into rotational components about three mutually perpendicular directions through the centre of gravity — the principal axes of rotation. Thus a body has three principal moment of inertia, one about each axis, usually designated as I_A , I_B and I_C .

Classification of molecules into the principal rotational classes →

The rotation of any three dimensional body is conveniently described in terms of rotations about three principal axes of inertia which are mutually at right angles and pass through the centre of gravity of the body. Thus the body has three principal 'moment of inertia' — one about each axis, conventionally designated I_A , I_B and I_C .

in order of increasing magnitude
($I_A < I_B < I_C$) ... On the basis
of P.I.F molecules ~~can~~ may be
classified into four groups according
to their shapes.

(i) Linear molecules \rightarrow

Example \rightarrow CO_2 , HCN , C_2H_2
 HCl , $\text{Cl}-\text{C}\equiv\text{C}-\text{H}$, OCS
etc.

These, as the name implies, are
the molecules in which all the
atoms are arranged in a straight
line. Three directions of rotations
(the principal axes of rotation)
may be taken as

(a) about the bond axis or

~~(b)~~ the molecular axis 'A'

(b) end-over-end rotation in
the plane of paper and
perpendicular to the ~~axis~~

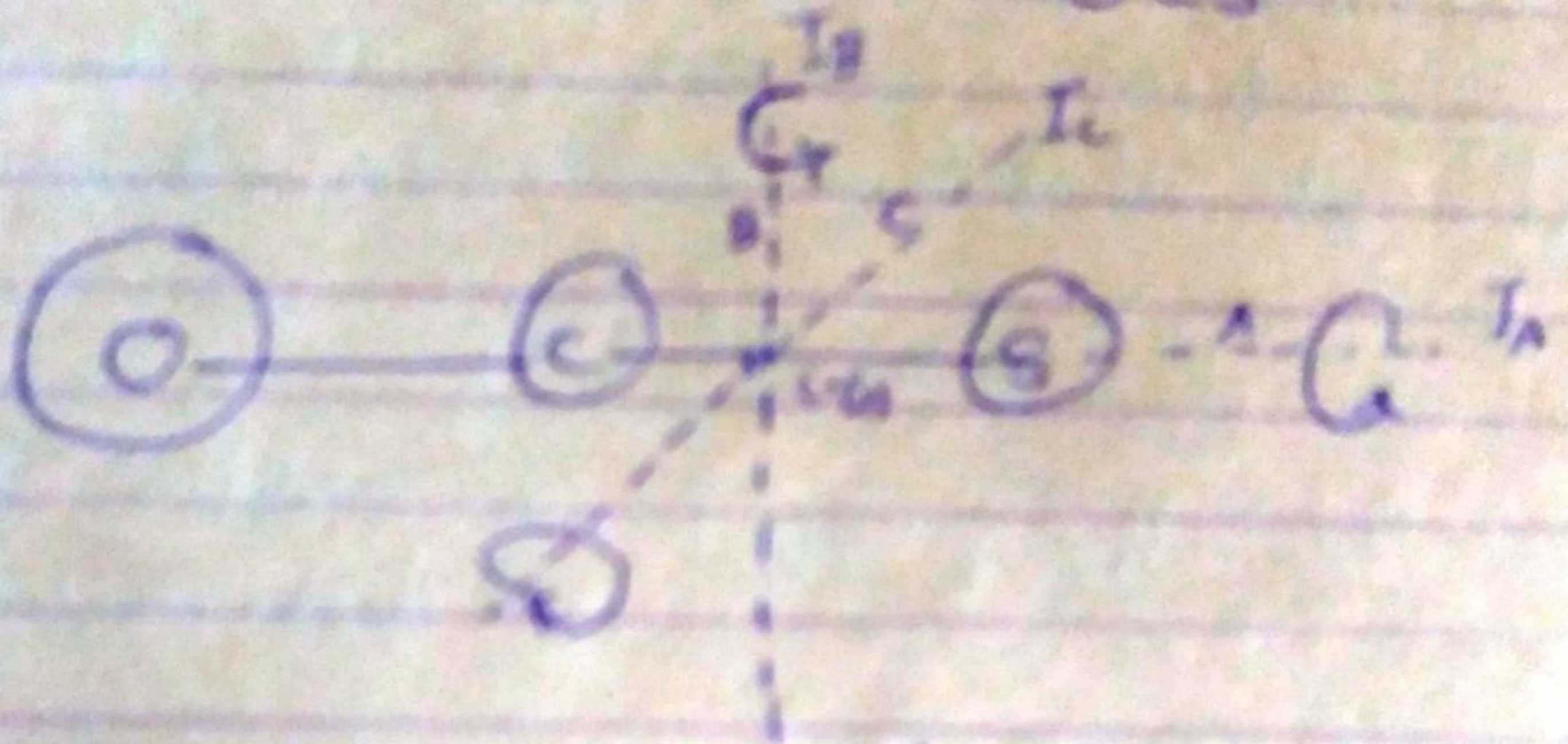
'A' molecular axis (A)

(c) end-over-end rotation
at right angles to the plane
i.e. perpendicular to the

both axes.

All the axes passing through the centre of gravity of the molecule.

For example — OCS



The principal axes of rotation is taken as I_A , I_B and I_C and corresponding to these axes is I_A , I_B and I_C .

Here, $I_A = 0$ since the nuclei on axis 'A' have practically all of the mass of the molecule.

$I_B = I_C$, it is also self evident that the moment of ~~inertia about~~ end-over-end rotation about the axes B, and C are the same.

so that $I_B = I_C$.

∴ Thus for linear molecule we have

$$I_B = I_C \text{ and } I_A = 0$$

The rotational spectra of this molecule is similar to that for diatomic molecule. And,

$$E = \bar{B} h c j(j+1)$$

$$\Delta E = 2\bar{B}$$

(modified by
distortion const.)

(2.) Symmetric tops molecules →

Example → NH_3 , BF_3 , C_6H_6
 CHCl_3 , CH_2Cl_2 , BCl_3
 CH_3F etc.

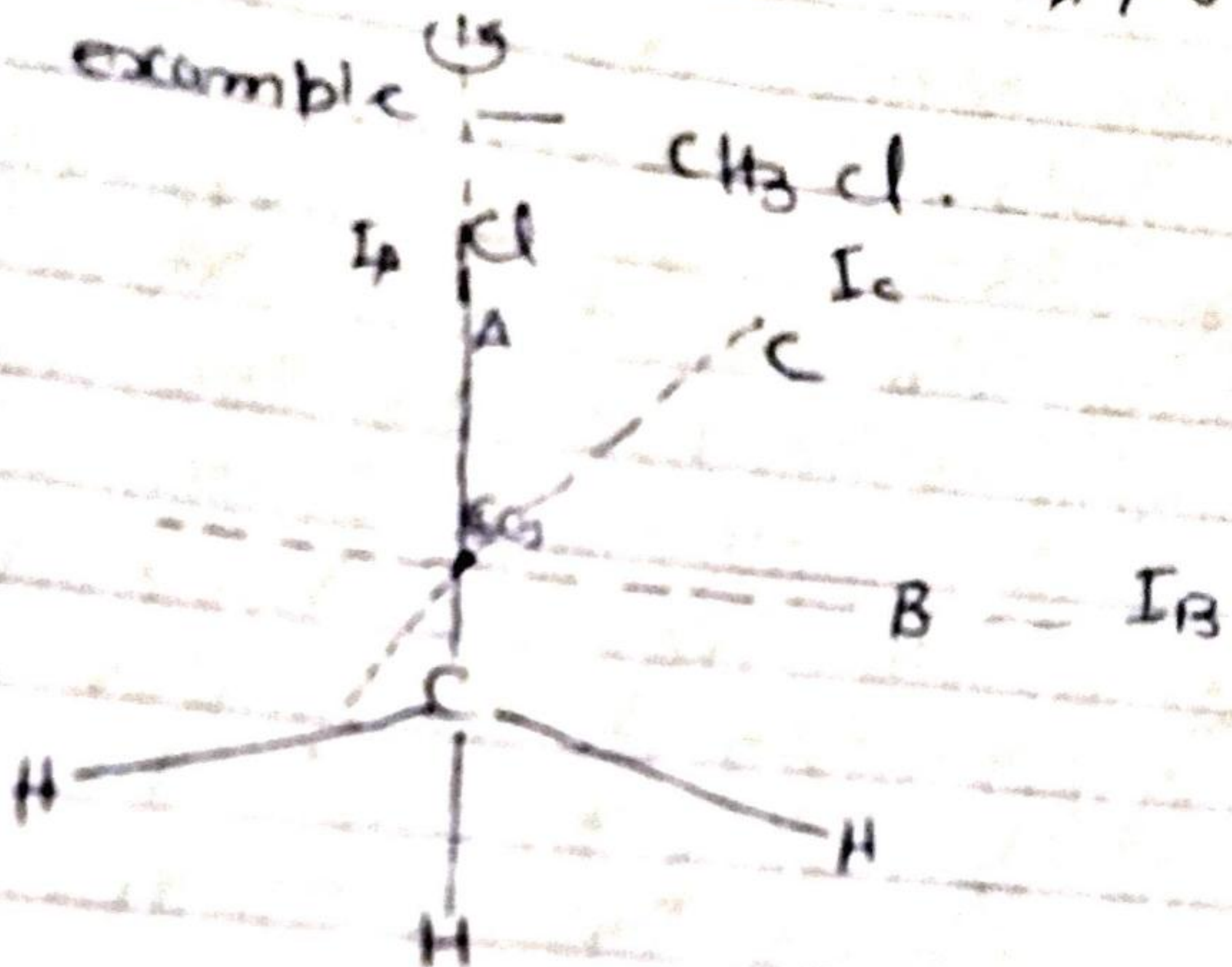
A symm. top molecule has ~~three~~ three non-zero moments of inertia two of which are equal. i.e.,

$$I_A \neq I_B = I_C \text{ or } I_A \neq I_B = I_C$$

For symmetric tops

$$I_B = I_C \neq I_A \quad \text{and} \quad I_A \neq 0$$

For example



It is umbrella-shaped with the three hydrogen atoms ~~be~~ bonded tetrahedrally to the carbon atom, as shown in figure. ~~As in the case of linear molecule~~ The principal axes of inertia are the C-Cl bond axis A, Oz , which the CG lies, and two mutually perpendicular axes B and C in a plane perpendicular ~~to~~ to the axis A. As in the case of linear molecules, the end-over-end rotation in, and out of the

plane of paper are still identical
 and we have $I_B = I_C$. The
 P.T. about the C-Cl bond
 axis (Chosen as the main principal
 axis since C-Cl is along it)
 is now not negligible, however,
 because it involves the rotation
 of three comparatively massive
 H-atoms off this axis.
 Such a molecule spinning about
 this axis resembles a spinning
 top, and hence the name of
 'Symmetric top' for the group.
~~There are two~~ we have
 them;

symmetric tops; $I_B = I_C \neq I_A$

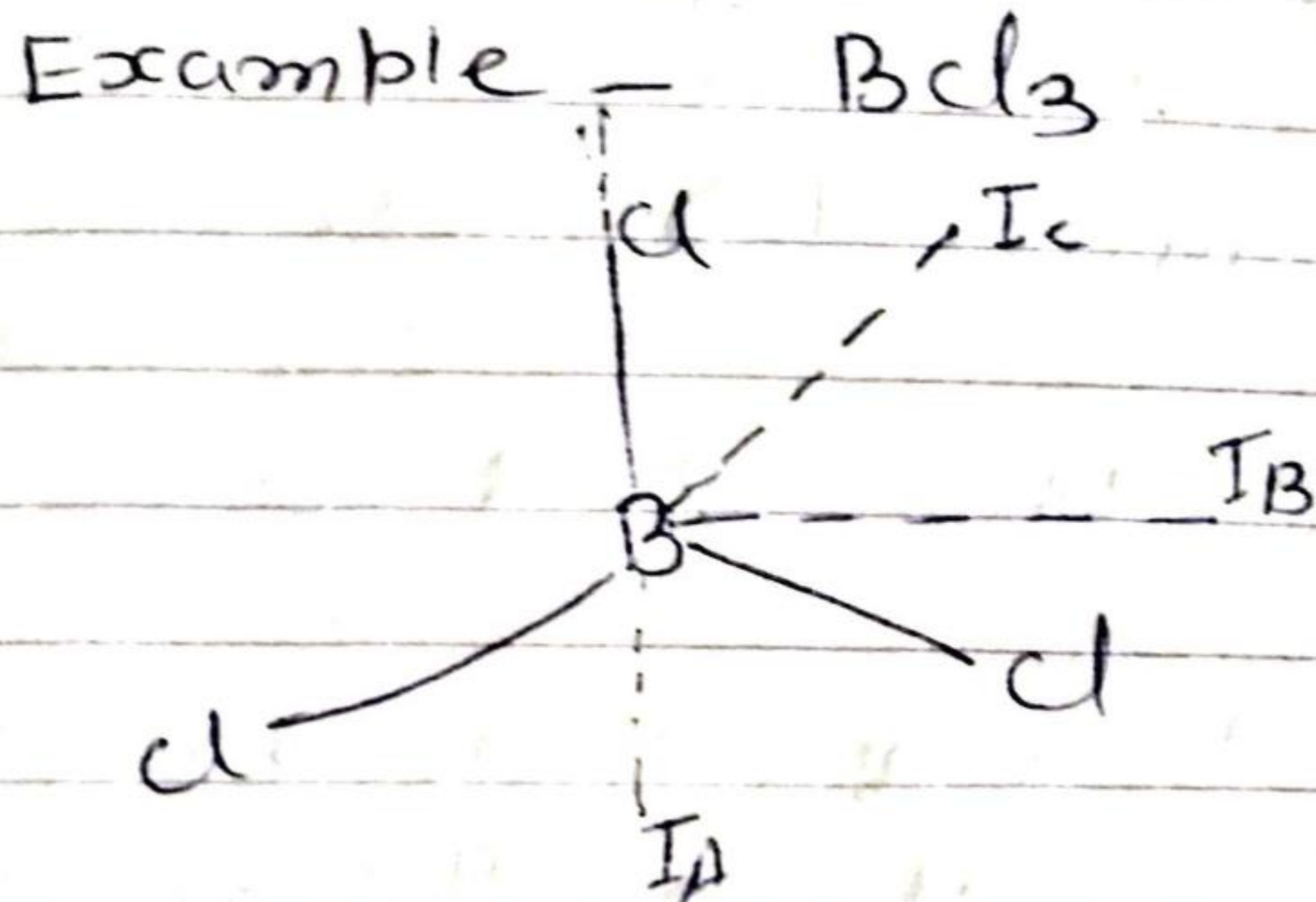
$$I_A \neq 0$$

There are two subdivisions of
 this class —

a) Prolate symmetric top \rightarrow
 if $I_A < I_B = I_C$ as in the
 above example CH_3Cl , the
 molecule is called Prolate

Symmetric top.

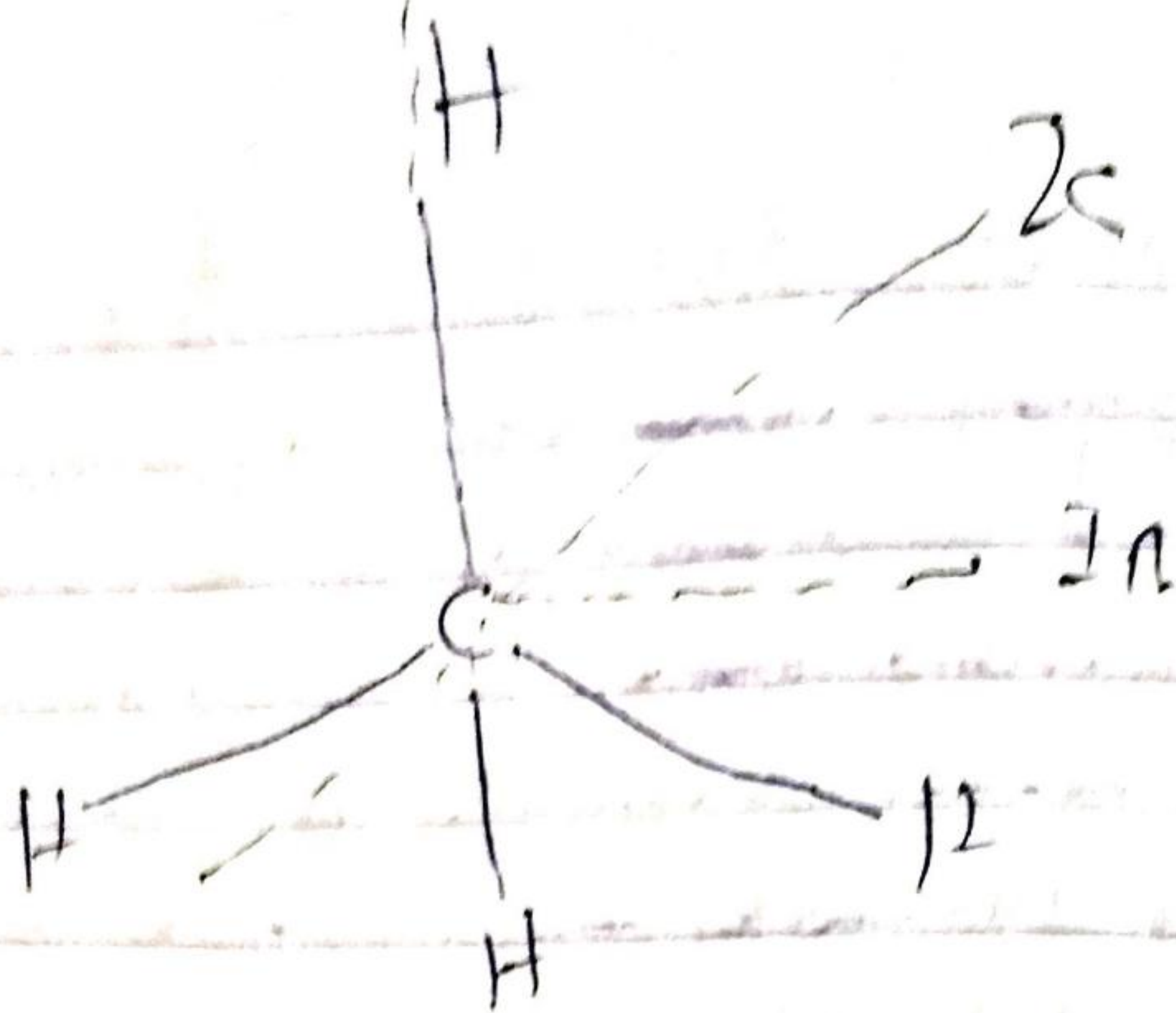
(b) Oblate symmetric top —
if $I_A > I_B = I_C$, it is
referred to as oblate symmetric top
molecule.



BCl_3 is planar and symmetrical
molecule. In this case

$$I_A = 2I_B = 2I_C$$

(3) Spherical top molecules →
When a molecule
has all three principal moment
of inertia identical, it is called
a spherical top. A simple
example is the tetrahedral molecule
methane CH_4 .



Spherical tops ;

$$I_A = I_B = I_C$$

gt magnetic moment ($\mu = 0$)
hence it is MW inactive.

Example - CH₄, SF₆ etc.

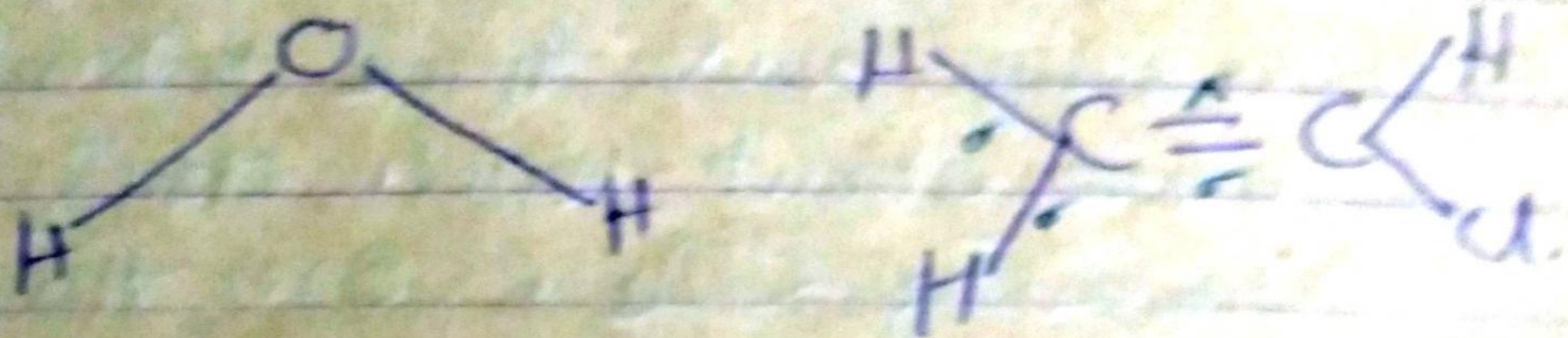
(A) Asymmetric tops ; -

When all the three principal moments of inertia are different the molecule is called an asymmetric top. i.e.,

$$I_A \neq I_B \neq I_C$$

The majority of substances belonging to this group.

Example \rightarrow H_2O , CH_3OH , vinyl chloride ($\text{CH}_2=\text{CHCl}$) etc.



An asymmetric top molecule has invariably dipole moment. Selection rule are only appropriate. Effects of centrifugal distortion are large. The rotational spectrum rich in line and complex. It is difficult to determine anything.
